

## Measures of Money

- Economists have developed di erent measures of money

M1 is a measure of the money supply; it consists of currency in the hands of the public plus traveler's checks, demand deposits, checking accounts, and other checkable deposits.
M2 is a measure of the money supply; it consists of M1 plus other relatively liquid assets (small denomination time deposits, savings deposits and money market deposit accounts, money market mutual fund shares)

Measures of the Monetary Aggregates in the USA

| Measures of the Monetary Aggregates |  |
| :---: | :---: |
|  | Value as of May 16, 2011 (S billions) |
| $\mathrm{Ml}=$ Currency | 958.8 |
| + Traveler's checks | 4.6 |
| + Demand deposits | 573.1 |
| + Other checkable deposits | 399.0 |
| Total M1 | 1,935.5 |
| $\mathrm{M} 2=\mathrm{M} 1$ |  |
| + Small-denomination time deposits | 848.3 |
| + Savings deposits and money market deposit accounts | 5,530.4 |
| + Money market mutual fund shares (retail) | 688.4 |
| Total M2 | 9,002.6 |

The more than $\$ 2,000$ of U.S. currency held per person in the United States is a surprisingly large number Where are all these dollars and who is holding them?

## Why People Hold Money

The only reason people would be willing to hold money is if they get some bene $t$ from doing so

- The transactions motive is the need to hold money for spending
- The precautionary motive is holding money for unexpected expenses and impulse buying
- The speculative motive is holding cash to avoid holding nancial assets whose prices are falling


Quantity of money

- The demand for money is downward-sloping: as the interest rate falls the cost of holding money falls
- When interest rates rise, bonds \& other nancial assets become more attractive, so you hold more of these \& less money


## Interest Rates and Present Value

A dollar paid to you one year from now is less valuable than a dollar paid to you today.

Why?

## Simple Interest

Simple interest is computed using the following formula:

$$
I=\operatorname{Pr}
$$

$I$ is the Interest, $P$ is the principal, and $r$ is the rate of interest.

Suppose you borrow $\$ 1000$ for a year at an annual interest rate of $9 \%$. How much interest will you owe the lender?

## Understanding Interest Rates

and
The Discounted Utility Model

The marshmallow test

## Interest Rates and Present Value

A dollar paid to you one year from now is less valuable than a dollar paid to you today.

Why?

A dollar deposited today can earn interest and become $\$ 1 \times(1+r)$ one year from today.

## Cost of credit

You borrow $\$ 1000$ (for a period of one year) with your Silver Axxess Visa Card. What is the total cost if this is the only charge to this card in this year?

Table 8.1 Credit-card offers for customers with bad credit

| Credit-card offer | APR | Fee |
| :--- | :---: | ---: |
| Silver Axxess Visa Card | $19.92 \%$ | $\$ 48$ |
| Finance Gold MasterCard | $13.75 \%$ | $\$ 250$ |
| Continental Platinum MasterCard | $19.92 \%$ | $\$ 49$ |
| Gold Image Visa Card | $17.75 \%$ | $\$ 36$ |
| Archer Gold American Express | $19.75 \%$ | $\$ 99$ |
| Total Tribute American Express | $18.25 \%$ | $\$ 150$ |
| Splendid Credit Eurocard | $22.25 \%$ | $\$ 72$ |

## Liability

The Liability L is:

$$
\begin{aligned}
L & =P+I \\
& =P+P r \\
& =P(1+r)
\end{aligned}
$$

## Implicit Interest

Suppose somebody o ers to lend you \$ 105 on the condition that you pay back \$ 115 one year later.

What is the interest rate $r$ ?

## Cost of credit

You borrow $\$ 1000$ (for a period of one year). Which credit card will cost the most to pay back?
Table 8.1 Credit-card offers for customers with bad credit

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## Exponential Discounting

People discount the future and hence prefer their rewards sooner than later.

Example: Tom prefers to have $\$ 100$ today rather than $\$ 100$ next year.

A person's time preference represents the extent to which they discount the future.

Exponential discounting is designed to capture this phenomenon.

## Exponential Discounting

Let $u>0$ be the utility you get from getting a dollar now.

Getting a dollar tomorrow is worth slightly less to you. Hence, we multiply it by a discount factor $\delta$ between 0 and 1 : $\delta u$

Getting a dollar the day after tomorrow is worth even less.
Thus, we multiply it by an additional $\delta: \delta^{2} u$

## Exponential Discounting

If we are interested in the entire utility stream
$u=\left\{u_{0}, u_{1}, u_{2}, \ldots\right\}$, the discounted utility from the point of view of time zero is given by the following expression:

$$
U^{0}(u)=\delta^{0} u_{0}+\delta^{1} u_{1}+\delta^{2} u_{2}+\ldots
$$

This is the delta function.

## Example

Table 8.2 Simple time-discounting problem

|  | $t=0$ | $t=1$ | $t=2$ |
| :---: | :---: | :---: | :---: |
| a | 1 |  |  |
| b |  | 3 |  |
| c |  |  | 4 |
| d | 1 | 3 | 4 |

Suppose $\delta=0.9$ and you are making a decision at $t=0$. What is the value of each choice?
What about if $\delta=0.1$ ?

## Examples


(a)

|  | $t=0$ | $t=1$ |
| :---: | :---: | :---: |
| $t=2$ |  |  |
| $\mathbf{a}$ |  | 6 |
| $\mathbf{b}$ |  | 3 |

(b)

(c)

You are indi erent between a and b . For each table, nd $\delta$.

## The Intertemporal Choice Model

- How would rational consumers distribute their consumption over time?
- Two time periods: current and future.
- Two alternatives (goods): current consumption (C1) versus future consumption (C2).


Utility of a future income


Figure 8.1 Exponential discounting

## Discount Factor $\delta$ and Discount Rate $r$

$$
\begin{aligned}
& r=\frac{1-\delta}{\delta} \\
& \delta=\frac{1}{1+r}
\end{aligned}
$$

## Intertemporal Budget Constraint with Income in

 Both Periods, and Borrowing or Lending at theRate $r$


## Marginal rate of time preference

the number of units of consumption in the future a consumer would exchange for 1 unit of consumption in the present.

- It declines as one moves downward along an indi erence curve.



## $c_{1}$

## Patience and Impatience


(a)

(b)

The Optimal Intertemporal Allocation


The e ect of a fall (or rise) in the interest rate depends on whether the consumer is a borrower or a saver.

- The income e ect...
- A borrower has more income after an interest rate fall. So, her income e ect is to consume more in both periods.
- A saver has less income after an interest rate fall. So, her income e ect is to consume less in both periods.
- The Substitution e ect after a fall in the interest rate is always to increase current consumption and reduce future consumption.



## Future Value: Compound Interest

$$
F V=P \times(1+r)^{t}
$$

You put $\$ 100$ into a savings account. Your bank promises an annual rate of $5 \%$.
What is your balance after 1 year?
10 years?
50 years?

You have an inheritance of $\$ 100,000$ you will receive in 10 years. What is it worth right now if the interest you could get on an investment is $4.5 \%$ (compounded annually)?

## Simple Present Value

$$
P V=\frac{C F}{(1+i)^{t}}
$$

You cannot directly compare payments scheduled in di erent points in the time line

|  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Year | 0 | $\$ 100$ | $\$ 100$ | 2 |
| PV | 100 | 1 | $100 /(1+\mathrm{i})$ | $100 /(1+\mathrm{i})^{2}$ |

What is better?
a Receiving \$100 in one year and \$200 in two years.
b Receiving \$340 in three years.
if the (constant) interest rate is $10 \%$ ?

Assume an annual interest rate of $7.5 \%$.
What is the Present Value of $\$ 10000$ received in (a) one year, (b) 5 years, and (c) 10 years?

## Net Present Value

$$
N P V=\sum_{0}^{T} \frac{B_{t}-C_{t}}{(1+r)^{t}}
$$

$B_{t}$ Cash in ow in period $t$
$C_{t}$ Cash out ow in period $t$
$r$ discount rate

You win the state lottery and will receive $\$ 100,000$ now and then each year for all eternity, i.e. your heirs will continue to receive the yearly payments once you die. For how much can you sell your prize right now?
Assume the annual interest rate will always be $2 \%$.

## Present Value of a Perpetuity

$$
\begin{aligned}
P & =\sum_{1}^{\infty} \frac{B}{(1+i)^{t}} \\
& =B \times \sum_{1}^{\infty} \frac{1}{(1+i)^{t}}=B \times \sum_{1}^{\infty}\left(\frac{1}{1+i}\right)^{t} \\
1+x+x^{2}+x^{3} \ldots & =\frac{1}{1-x} \quad \forall x<1 \\
P & =B \times\left(\frac{1}{1-1 /(1+i)}-1\right) \\
& =B \times\left(\frac{1-1+1 /(1+i)}{1-1 /(1+i)}\right) \\
& =B \times\left(\frac{1 /(1+i)}{(1+i-1) /(1+i)}\right) \\
& =B \times \frac{1}{i}
\end{aligned}
$$

## Yield to Maturity Internal Rate of Return

The interest rate that equates the present value of cash ow payments received from a debt instrument with its value today

## Fixed Payment Loan

The same cash flow payment every period throughout
the life of the loan

$$
\mathrm{LV}=\text { loan value }
$$

FP = fixed yearly payment
$n=$ number of years until maturity

$$
\mathrm{LV}=\frac{\mathrm{FP}}{1+i}+\frac{\mathrm{FP}}{(1+i)^{2}}+\frac{\mathrm{FP}}{(1+i)^{3}}+\ldots+\frac{\mathrm{FP}}{(1+i)^{n}}
$$

Four Types of Credit Market Instruments

- Simple Loan
- Fixed Payment Loan
- Coupon Bond
- Discount Bond


## Simple Loan

$$
\begin{gathered}
\mathrm{PV}=\text { amount borrowed }=\$ 100 \\
\mathrm{CF}=\text { cash flow in one year }=\$ 110 \\
n=\text { number of years }=1
\end{gathered}
$$

$$
\$ 100=\frac{\$ 110}{(1+i)^{1}}
$$

$$
(1+i) \$ 100=\$ 110
$$

$$
(1+i)=\frac{\$ 110}{\$ 100}
$$

$$
i=0.10=10 \%
$$

For simple loans, the simple interest rate equals the yield to maturity

## Bonds

- A bond is a sophisticated IOU that documents who owns how much and when payment must be paid.
- Issuing bonds allows borrowing directly from the public.
- Lender: one who buys a bond
- Borrower: one who issues a bond
- Corporations and governments at all levels borrow money by issuing bonds.
- All bonds involve a risk.
- Major issues are graded by rating companies: Standard and Poor's, Moody's
- Grades range from lowest risk (AAA) bonds in current default (D)
- The higher the risk the greater the interest rate required to get lenders to buy the bonds.


A coupon payment on a bond is a periodic interest payment that the bondholder receives during the time between when the bond is issued and when it matures.

|  |  |
| :---: | :---: |
| Yields to Maturity on a 10\%-Coupon-Rate Bond <br> Maturing in Ten Years (Face Value $=\$ 1,000$ ) Yields to Maturity on a $10 \%$-Coupon-Rate Bond Maturing in Ten Years (Face Value $=\$ 1,000$ ) |  |
| ( Bond (s) | to Maturit |
| 1.200 | ${ }^{7} 13$ |
| 1,1,00 1,000 | 8.48 10.00 1 |
| 900 | 11.75 |
| 800 | 13.81 |

- When the coupon bond is priced at its face value, the yield to maturity equals the coupon rate
- The price of a coupon bond and the yield to maturity are negatively related
- The yield to maturity is greater than the coupon rate when the bond price is below its face value


## Discount Bond Zero Coupon Bond

- No interest payments (=coupons)
- Sold for a price below face value
- US Treasury Bills are examples of such Zero Coupon Bonds
- Some zero coupon bonds are in ation indexed, the nominal face value is in ation adjusted
- Short term zero coupon bonds are called Bills


## Coupon Bond

Using the same strategy used for the fixed-payment loan:

$$
\begin{gathered}
\mathrm{P}=\text { price of coupon bond } \\
\mathrm{C}=\text { yearly coupon payment } \\
\mathrm{F}=\text { face value of the bond } \\
n=\text { years to maturity date } \\
\mathrm{P}=\frac{\mathrm{C}}{1+i}+\frac{\mathrm{C}}{(1+i)^{2}}+\frac{\mathrm{C}}{(1+i)^{3}}+\ldots+\frac{\mathrm{C}}{(1+i)^{n}}+\frac{\mathrm{F}}{(1+i)^{n}}
\end{gathered}
$$

## Consol or Perpetuity

- A bond with no maturity date that does not repay principal but pays xed coupon payments forever

$$
P=C / i
$$

$P$ Price of consol
$C$ yearly interest payment
$i$ yield to maturity

$$
i=C / P
$$

- For coupon bonds, this equation gives the current yield, an easy to calculate approximation to the yield to maturity


## Discount Bond

For any one year discount bond

$$
i=\frac{\mathrm{F}-\mathrm{P}}{\mathrm{P}}
$$

$\mathrm{F}=$ Face value of the discount bond
$\mathrm{P}=$ current price of the discount bond
The yield to maturity equals the increase in price over the year divided by the initial price. As with a coupon bond, the yield to maturity is negatively related to the current bond price.

## Interest Rates vs Rate of Returns

Rate of Return
The payments to the owner plus the change in value expressed as a fraction of the purchase price

$$
\mathrm{RET}=\frac{\mathrm{C}}{\mathrm{P}_{t}}+\frac{\mathrm{P}_{t+1}-\mathrm{P}_{t}}{\mathrm{P}_{t}}
$$

RET $=$ retum from holding the bond from time $t$ to time $t+1$

$$
\mathrm{P}_{t}=\text { price of bond at time } t
$$

$\mathrm{P}_{t+1}=$ price of the bond at time $t+1$

$$
\mathrm{C}=\text { coupon payment }
$$

$$
\frac{\mathrm{C}}{\mathrm{P}_{\mathrm{s}}}=\text { current yield }=i_{c}
$$

$$
\frac{\mathrm{P}_{t+1}-\mathrm{P}_{t}}{\mathrm{P}_{t}}=\text { rate of capital gain }=g
$$

## One-Year Returns on Di erent-Maturity 10\%-Coupon-Rate Bonds When Interest Rates Rise from $10 \%$ to $20 \%$



## The Distinction Between Real and Nominal Interest Rates

Nominal interest rate makes no allowance for in ation Real interest rate is adjusted for changes in price level so it more accurately re ects the cost of borrowing Ex ante real interest rate is adjusted for expected changes in the price level Ex post real interest rate is adjusted for actual changes in the price level

## The Distinction Between Interest Rates and

## Returns

- The return equals the yield to maturity only if the holding period equals the time to maturity
- A rise in interest rates is associated with a fall in bond prices, resulting in a capital loss if time to maturity is longer than the holding period
- The more distant a bond's maturity, the greater the size of the percentage price change associated with an interest-rate change
- The more distant a bond's maturity, the lower the rate of return the occurs as a result of an increase in the interest rate
- Even if a bond has a substantial initial interest rate, its return can be negative if interest rates rise


## Interest-Rate Risk

Prices and returns for long-term bonds are more volatile than those for shorter-term bonds There is no interest-rate risk for any bond whose time to maturity matches the holding period

## Fisher Equation

Real and Nominal Interest Rates (Three-Month Treasury Bill), 19532011

Interest Rate
(\% annual rate)


Sources: Nominal rates from
www.federalreserve.gov/releases/H15 and in ation from ftp://Sources: Nominal rates from www.federalreserve.gov/releases/H15 and in ation from

